



Website



Paper



Code



Video

B*: Efficient and Optimal Base Placement for Fixed-Base Manipulators



Zihang Zhao^{1,2,3,6,*}, Leiyao Cui^{2,5,*}, Sirui Xie^{1,2,3,*}, Saiyao Zhang^{2,5}, Zhi Han⁵, Lecheng Ruan⁴, and Yixin Zhu^{1,2,3,†}

¹Institute for Artificial Intelligence, Peking University ²School of Psychological and Cognitive Sciences, Peking University

³Beijing Key Laboratory of Behavior and Mental Health, Peking University ⁴College of Engineering, Peking University

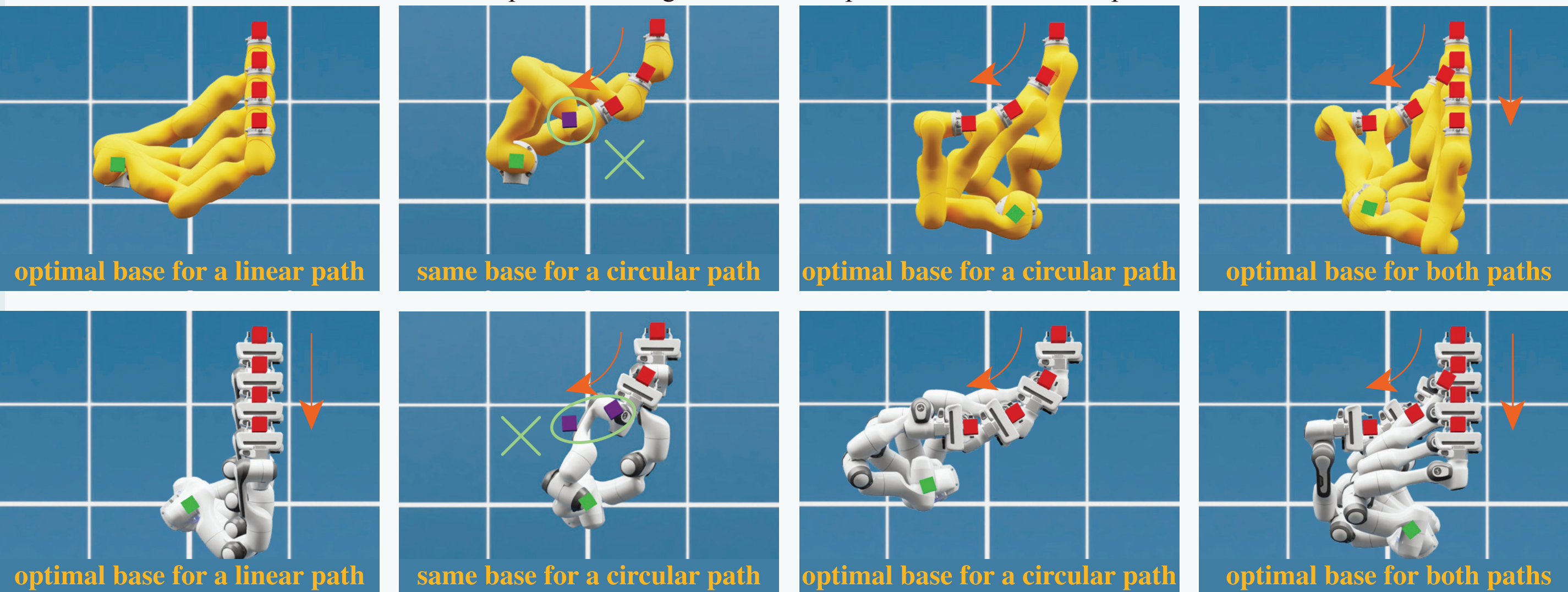
⁵University of Chinese Academy of Sciences, Beijing ⁶LeapZenith AI Research, Shanghai *Equal contributors †Corresponding author



Motivation

Base placement is task-dependent

■ base pose ■ target end-effector pose ■ unreachable pose



• **Input:** An ordered sequence of desired end-effector poses

$$\mathbf{x}_{1:t} = [\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_t] \in \mathbb{R}^{t \times 6}$$

• **Output:** An optimal base placement $\mathbf{q}^b = [x^b, y^b, \theta^b]^T \in \text{SE}(2)$ and feasible joint configurations $\mathbf{q}_{1:t}^m = [q_1, q_2, \dots, q_t] \in \mathbb{R}^{t \times n}$

Non-convex workspace

Robot workspaces are riddled with discontinuities, singularities, and uneven dexterity, making base placement inherently non-convex.

Task & robot dependency

The optimal base varies with both robot kinematics and task — one task's best placement can make another infeasible.

Multi-constraint requirements

Valid placement must jointly satisfy path-wide reachability, joint continuity, collision avoidance, and task-specific goals across long horizons.

Current methods' limitations

Solution optimality



Computational efficiency

Method

Base placement formulation

$$\begin{aligned} & \text{minimize}_{\mathbf{q}^b, \mathbf{q}_{1:t}^m} f(\mathbf{q}^b, \mathbf{q}_{1:t}^m) = \sum_{i=1}^{t-1} \|\mathbf{q}_{i+1}^m - \mathbf{q}_i^m\|_1 \\ & \text{subject to } \psi(\mathbf{q}^b, \mathbf{q}_i^m) = \mathbf{x}_i, \quad i = 1, 2, \dots, t \\ & \quad \mathbf{q}^{b^m} \preceq \mathbf{q}^b \preceq \mathbf{q}^{b^M}, \\ & \quad \mathbf{q}^{m^m} \preceq \mathbf{q}_i^m \preceq \mathbf{q}^{m^M}, \quad i = 1, 2, \dots, t \\ & \quad \text{sd}(\mathbf{q}^b, \mathbf{q}_i^m) \geq 0, \quad i = 1, 2, \dots, t \end{aligned}$$

Base relaxation

$$\mathbf{q}^b \rightarrow \mathbf{q}_{1:t}^b$$

Relax problem by treating the fixed base as mobile

Constraint tightening

$$f'(\mathbf{q}_{1:t}^b, \mathbf{q}_{1:t}^m, \mu(j)) = f(\mathbf{q}_{1:t}^b, \mathbf{q}_{1:t}^m) + \mu(j) \sum_{i=1}^t \|\mathbf{q}_i^b - \bar{\mathbf{q}}^b\|_1$$

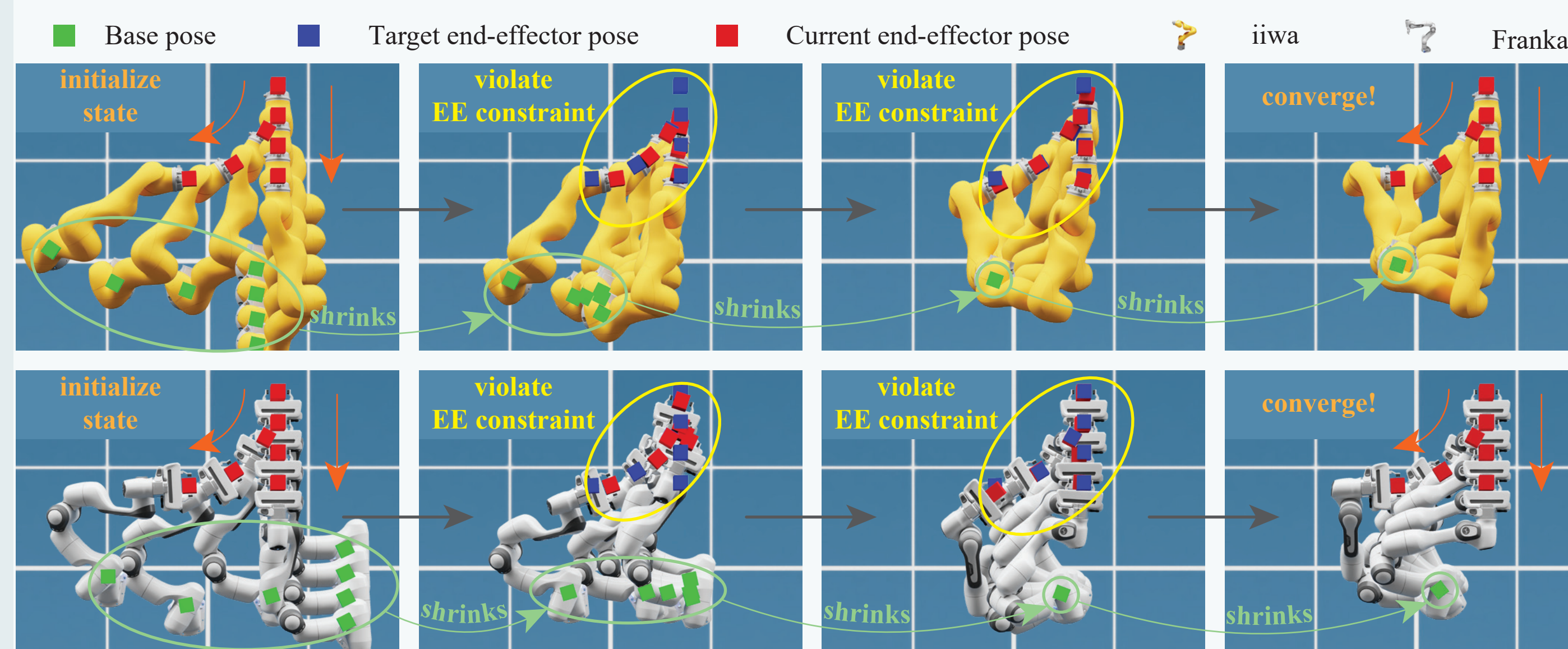
Penalize base movement with an iteration-dependent coefficient

Sequential linearization

$$\phi_c(x) = \phi(x_0) + \dot{\phi}(x_0)(x - x_0)$$

Solve sequential LP subproblems inside adaptive trust regions

Visualization of B* optimization process



Validation

100%

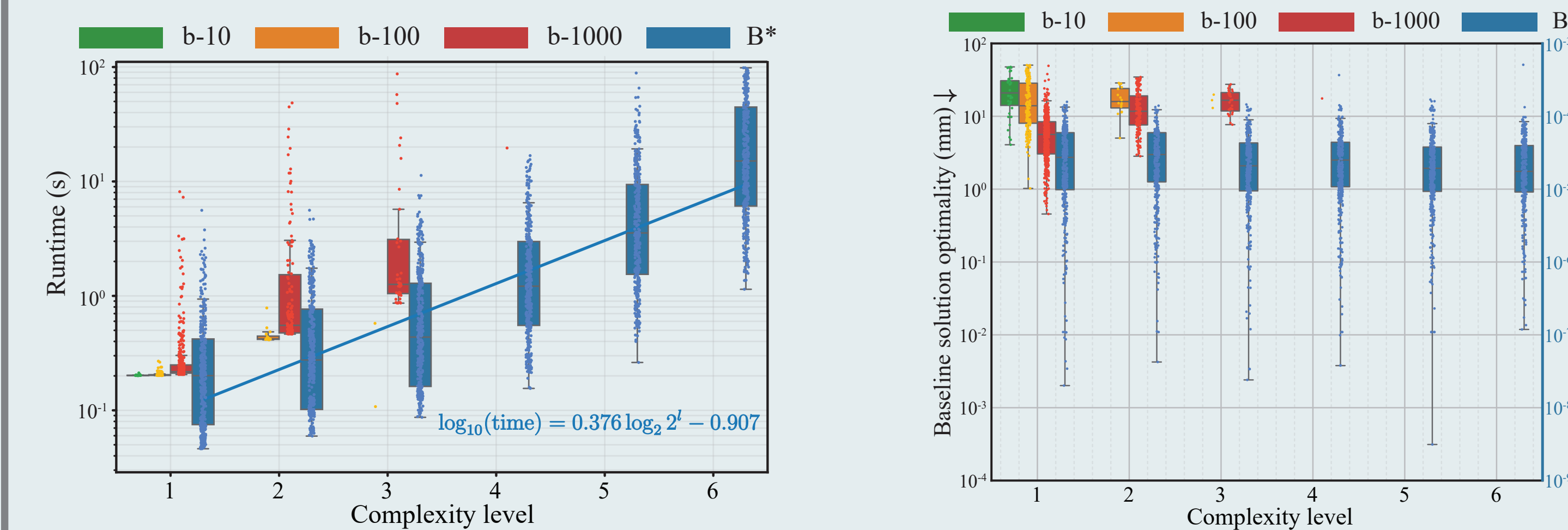
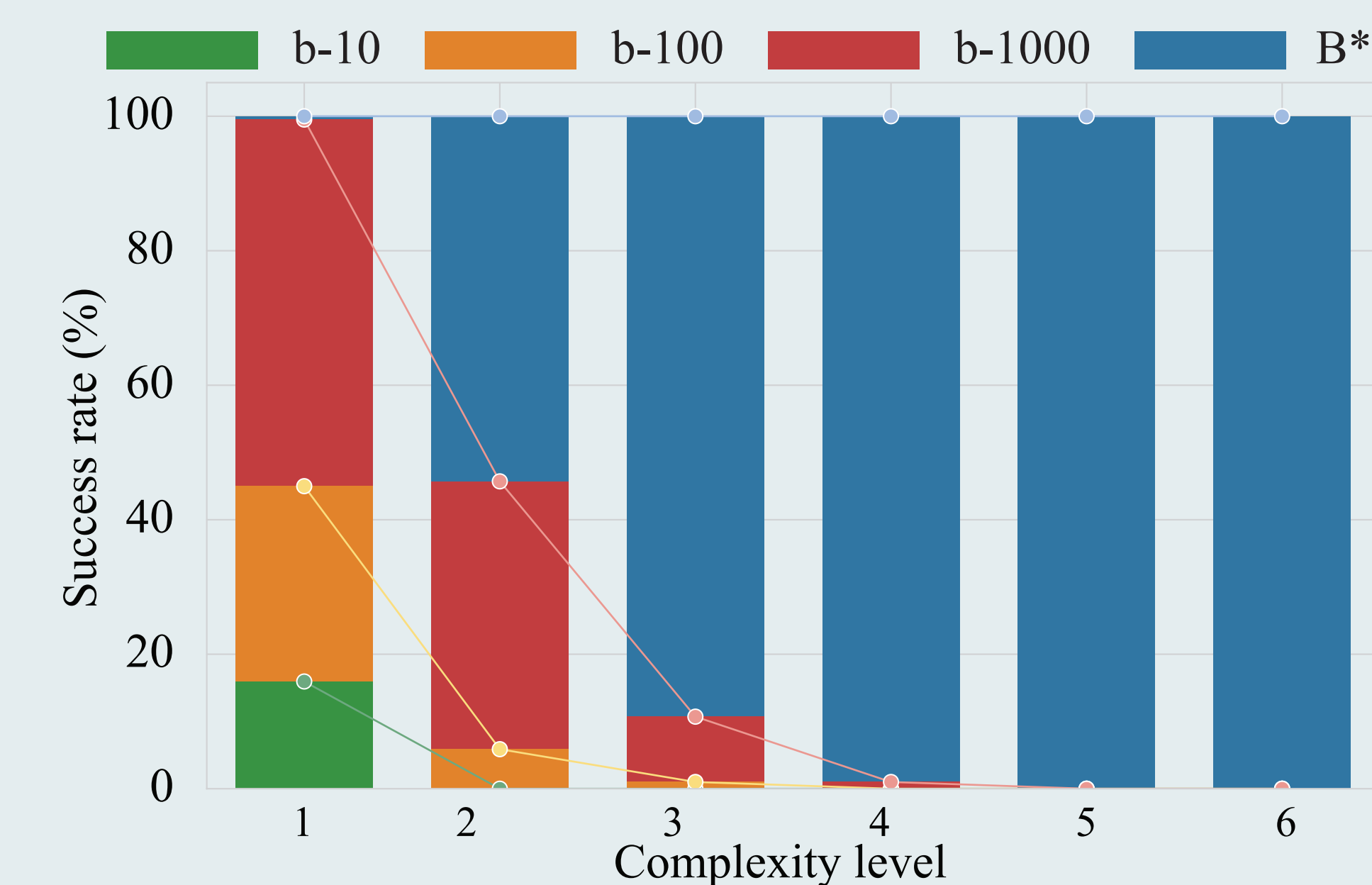
valid solutions on all 2,400 generated tasks

10⁵x

lower base ATE than baselines

2,400

random trajectories, six complexity levels



B* outperforms baselines, achieving a 100% success rate, higher precision, and superior runtime efficiency.

Real-world validation

